# Isomeric yield ratio measurements for fission dynamics

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#### **Outline**

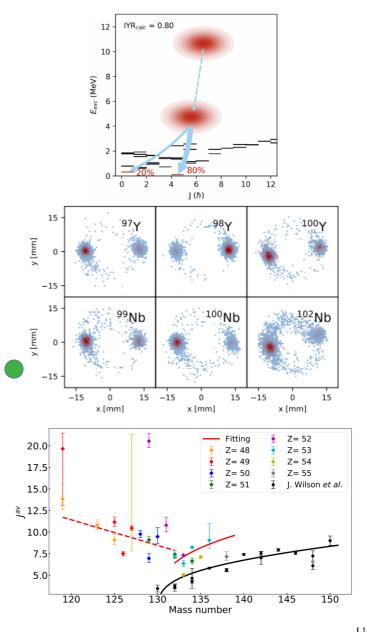
Motivation and background
Isomeric yield ratios (IYRs) for studying
angular momenta of fission fragments

**Experimental** approach and ...

... results from IGISOL for <sup>232</sup>Th(α,f) highlighting the impact of CN angular momentum ■ ... with special attention to the <sup>98</sup>Y region ■

Linking isomeric yields to fission fragment angular momenta

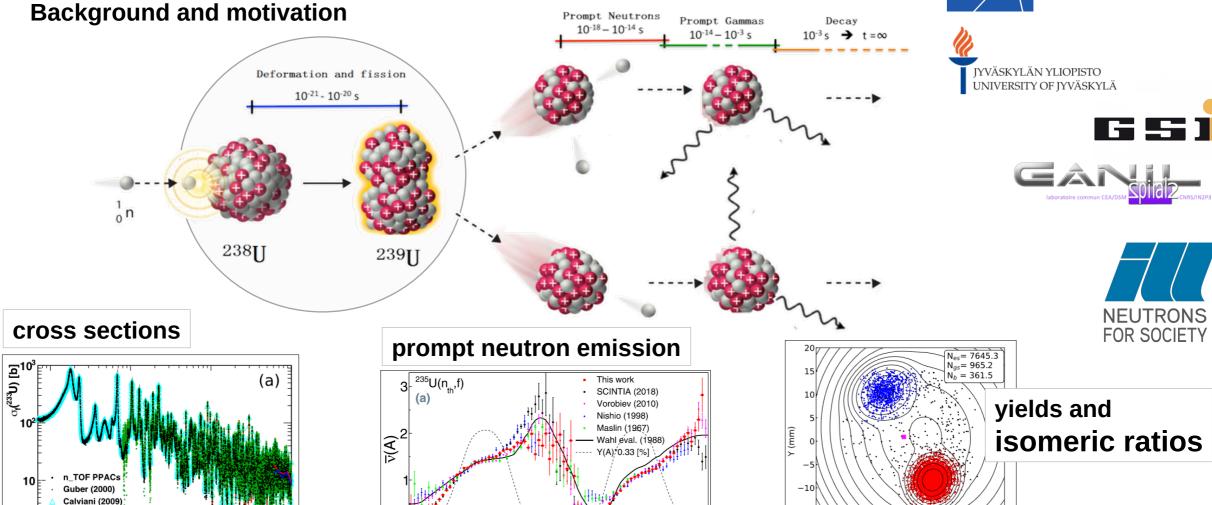
**Summary and outlook** 











140

D. Tarrío et al, Phys. Rev. C 107, 044616 (2023)

10

ENDF/B-VIII.0

A. Al-Adili et al, Phys. Rev. C **102**, 064610 (2021)

100

120 A pre (u)

Z. Gao et al, Phys. Rev. C **108**, 054613 (2023)

X (mm)

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En [eV] 10<sup>3</sup>

Somehow the fission fragments are tumbling apart after scission. What makes them do so?

Already before the experimental evidence for these surprisingly large angular momenta there where theories suggesting

- pre-fission angular momentum generation;
   collective vibrations; wriggling, bending, twisting;
   see e.g. J. Randrup and R. Vogt and the FREYA code
- **post-scission** models Coulomb forces; microscopic theories (e.g. Bertsch et al. 2019)

PHYSICAL REVIEW C

VOLUME 5, NUMBER 6

JUNE 1972

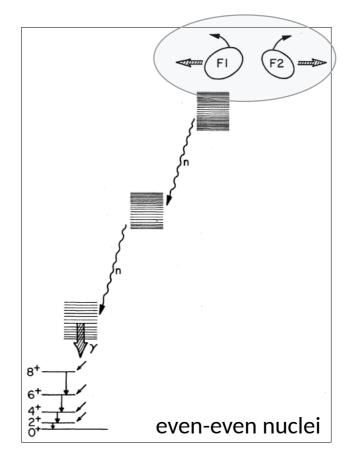
#### Angular Momentum of Primary Products Formed in the Spontaneous Fission of <sup>252</sup>Cf<sup>†</sup>

J. B. Wilhelmy, \* E. Cheifetz, ‡ R. C. Jared, S. G. Thompson, and H. R. Bowman Lawrence Berkeley Laboratory, University of California, Berkeley, California 94720

and

#### J. O. Rasmussen

Chemistry Department, Yale University, New Haven, Connecticut 06520 (Received 22 November 1971)





#### **Angular momentum of fission fragments**

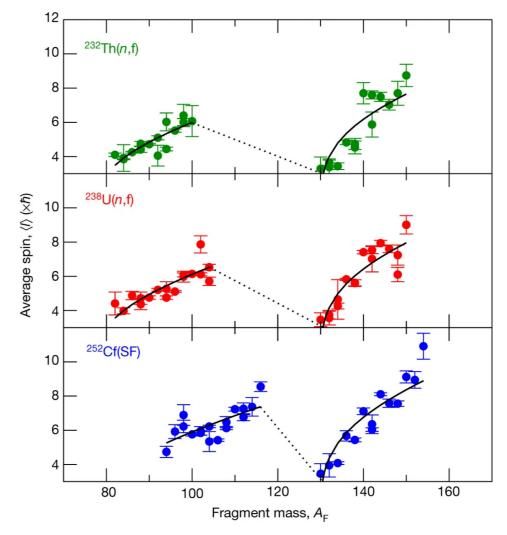
The debate got fresh fuel with the results from J. Wilson et al., Nature **590**, 566 (2021).

All three studied systems showed the same sawtooth-like behaviour\*.

#### Furthermore:

"Here we show that there is **no significant correlation** between the spins of the fragment partners, which leads us to conclude that angular momentum in fission is actually **generated after the nucleus splits (post-scission)**."

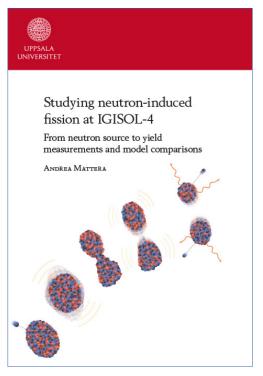
Several subsequent papers challenged this conclusion, e.g., Randrup&Vogt, PRL 127, 062502 (2021).





<sup>\*</sup> Based on gamma-spectrometry of side-feeding in 0+-nuclei.

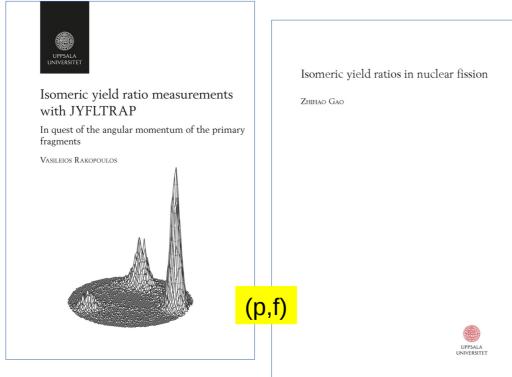
## We study <u>isomeric yield ratios</u> from fission to address this quest of angular momentum generation



EPJ A (2017) **53**: 173

EPJ A (2018) **54**: 33

(n,f)



From scission to metastability
Isomeric yield ratios in fission studies

Simone Cannarozzo

PRC **98** 024612 (2018) PRC **99** 014617(2019)

EPJ A (2022) **58**: 27 EPJ A (2023) **59**: 169 PRC **108** 054613 (2023) PRC **109** 064626 (2024) EPJ A (2023) **59**: 295 PRC **111** L031601 (2025) Manuscript submitted to PLB





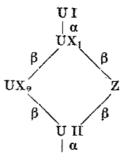
#### **Isomers from fission**

The existence of nuclear isomers Was suggested already 1917 by Frederick Soddy as "a finer degree of isotopy".

They were experimentally discovered by Otto Hahn 104 years ago.

Today about 2500 isomers with half-lives larger than **10 ns** are known.

Falls UX<sub>1</sub> die Muttersubstanz ist, dann muß die Ausbeute an Z aus UX-Präparaten mit der Halbwertszeit des UX<sub>1</sub>, also rund 24 Tagen, abnehmen. Ob dies tatsächlich der Fall ist, konnte noch nicht genau festgestellt werden. Versuche darüber sind im Gange. Falls sich diese genetische Beziehung bestätigt, so muß man für das UX<sub>1</sub> einen dualen Zerfall annehmen, wie ihn das folgende Schema veranschaulicht:

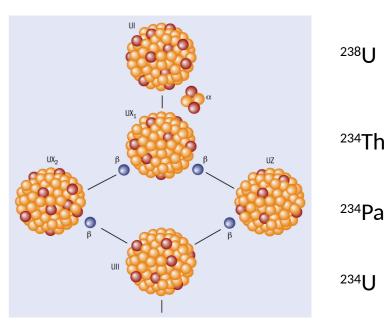


Sollte es sich dagegen herausstellen, daß UX<sub>1</sub> nicht die Muttersubstanz von Z ist, so hätte man ein mit UX<sub>1</sub> isotopes Produkt anzunehmen, für dessen Ursprung dann nur ein neues Uranisotop UIII in Frage käme. Dieses wäre dann vermutlich die Ausgangssubstanz für eine neue Reihe radioaktiver Zerfallsprodukte, deren einzelne Glieder sich unter die entsprechenden isotopen Glieder der Uran-Radium-Reihe mischten, und die man bei ihrer geringen Intensität bisher sehr wohl hätte übersehen können. Auf die mancherlei sich hieraus ergebenden Folgerungen sei hier vorerst nicht eingegangen, weil ja das Experiment in nicht zu langer Zeit entscheiden wird, welche der beiden Entstehungsmöglichkeiten von Z den Tatsachen entspricht.

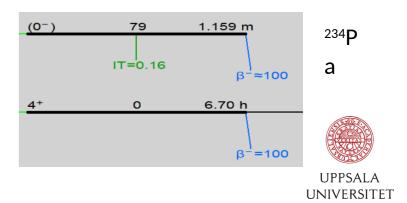
Berlin-Dahlem, den 21. Januar 1921.
Otto Hahn,

Kaiser-Wilhelm-Institut für Chemie.

Hahn, Otto: "Über ein neues radioaktives Zerfallsprodukt im Uran", Die Naturwissenschaften **9**, 84 (1921) doi:10.1007/BF01491321

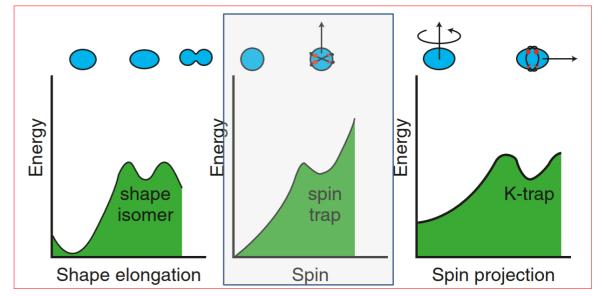


Ph. Walker and Zsolt Podolyák: "Celebrating a centrury of nuclear isomers", Physics World, April 2021.



#### Isomers from fission and fragment angular momenta

Relative population of different spin states, reflects the angular momentum of a fission fragment decaying into either of these states.



PHYSICAL REVIEW

VOLUME 120, NUMBER 4

NOVEMBER 15, 1960

#### Interpretation of Isomeric Cross-Section Ratios for $(n,\gamma)$ and $(\gamma,n)$ Reactions\*

J. R. Huizenga and R. Vandenbosch Argonne National Laboratory, Argonne, Illinois (Received July 11, 1960)

The relative probability of forming each member of a pair of nuclear isomeric states has been compared with theoretical predictions in order to learn which nuclear parameters can be determined from these data. For thermal neutron capture reactions, the observed ratios do not give much information about the dependence of the nuclear level density on spin, but they are consistent with a spin cutoff factor,  $\exp[-(J+\frac{1}{2})^2/2\sigma^2]$ , where  $\sigma \leq 5$ . The calculations are sufficiently consistent with experiment to make their predictions usable as a guide for assigning spins to

#### 1. INTRODUCTION

THE relative probability of forming each state of an isomeric pair seems to be governed mainly

\* Based on work performed under the auspices of the U. S. Atomic Energy Commission. the compound states formed in thermal or resonant energy neutron capture. For  $(\gamma,n)$  reactions, the calculations reproduce the energy dependence of the experimentally observed isomeric cross-section ratios. In order to obtain quantitative information about the spin dependence of the nuclear level density, it is necessary to consider reactions where particles are emitted which can carry off enough angular momentum to reach many spin states of the residual nucleus.

by the spin differences between the states which decay to the isomers and the isomer spins themselves. In the many cases (encountered in radioactivity) in which a third low-lying state can decay to either of the isomers, the well-known preference of the photon transition of

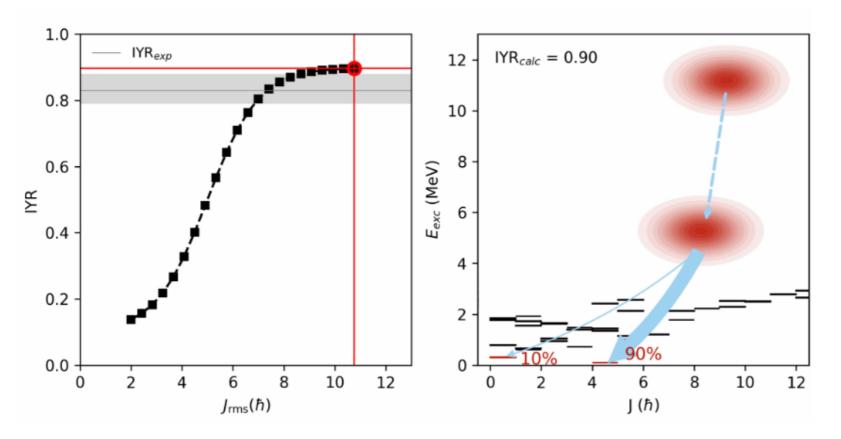
Walker & Dracoulis, "Energy traps in atomic nuclei", Nature **399**, 35 (1999) https://doi.org/10.1038/19911



## Isomers from fission and fragment angular momenta

- 1) Measure IYR, i.e., relative population of (long-lived) isomers.
- 2) Develop methods to "back-track" and determine  $J_{rms}$  of fragments.

$$IYR = \frac{Y_{high \ spin}}{Y_{high \ spin} + Y_{low \ spin}}$$



Fission fragment

Prompt neutron emission

Fission product

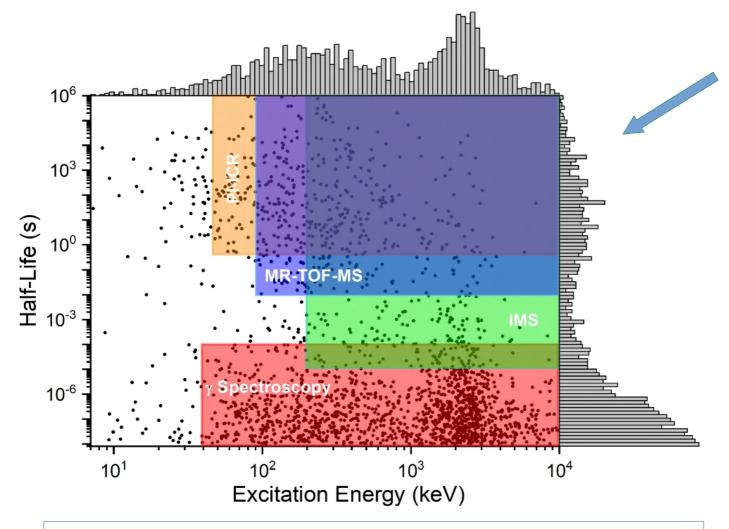
Prompt gamma emission



# **Experimental approach**



## Possible measurement techniques for IYR



Dickel, T., Mollaebrahimi, A., Eur. Phys. J. Spec. Top. 233, 1181–1190 (2024)

#### We use direct ion counting,

i.e., mass measurement techniques like phase-imaging ion-cyclotron-resonance (PI-ICR) and multi-reflection time-of-flight (MR-TOF)

These techniques offer a significant advantage compared to techniques using  $\gamma$ -ray spectroscopy, since we do not rely on available knowledge of the nuclear level schemes.

However, these techniques require relatively "long" half-lives.

This is pioneered by the Uppsala group in collaboration with the IGISOL group at the University of Jyväskylä, Finland.

See, e.g., Rakopoulos et al PRC 2018 and 2019, and R. Korkiamäki, MSc thesis, University of Jyväskylä (2024)

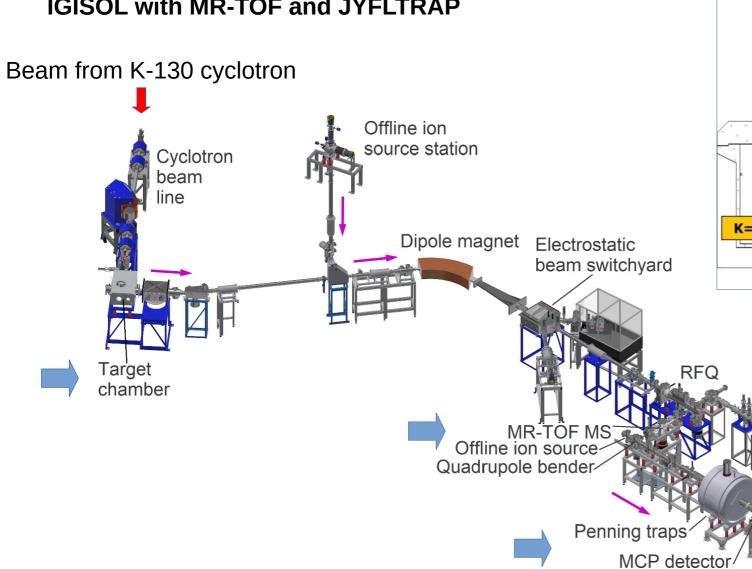
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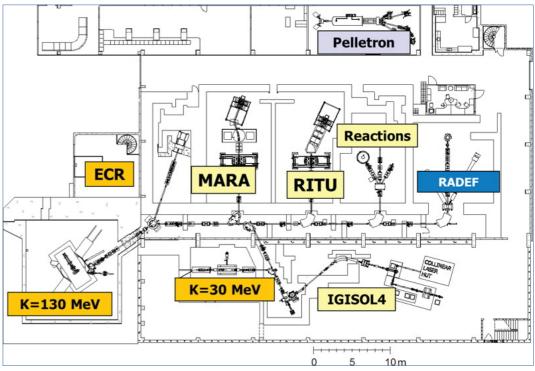
# Let's go to Jyväskylä in Finland! [Mennään Jyväskylään Suomessa!]





#### **IGISOL** with MR-TOF and JYFLTRAP



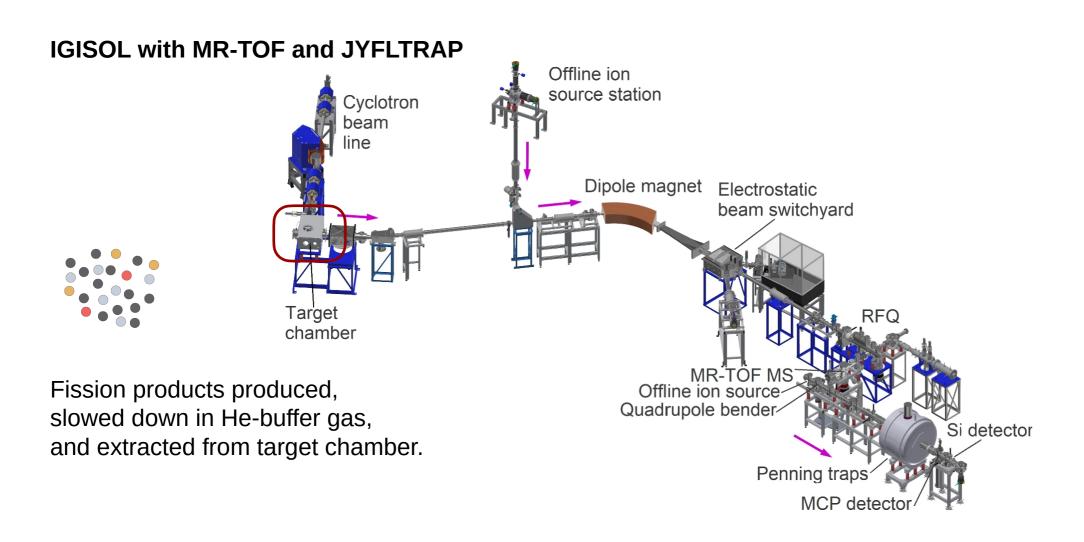


Ari Jokinen, Nuclear Physics News 24(4), 2014 https://doi.org/10.1080/10619127.2014.972165

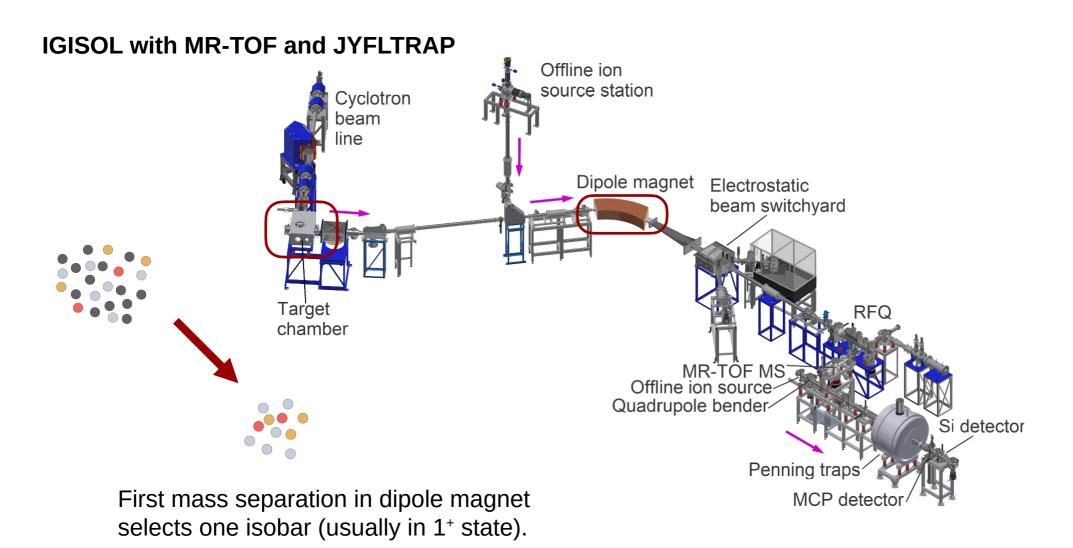
The lab is well-known for, e.g., high-precision mass measurements

Si detector



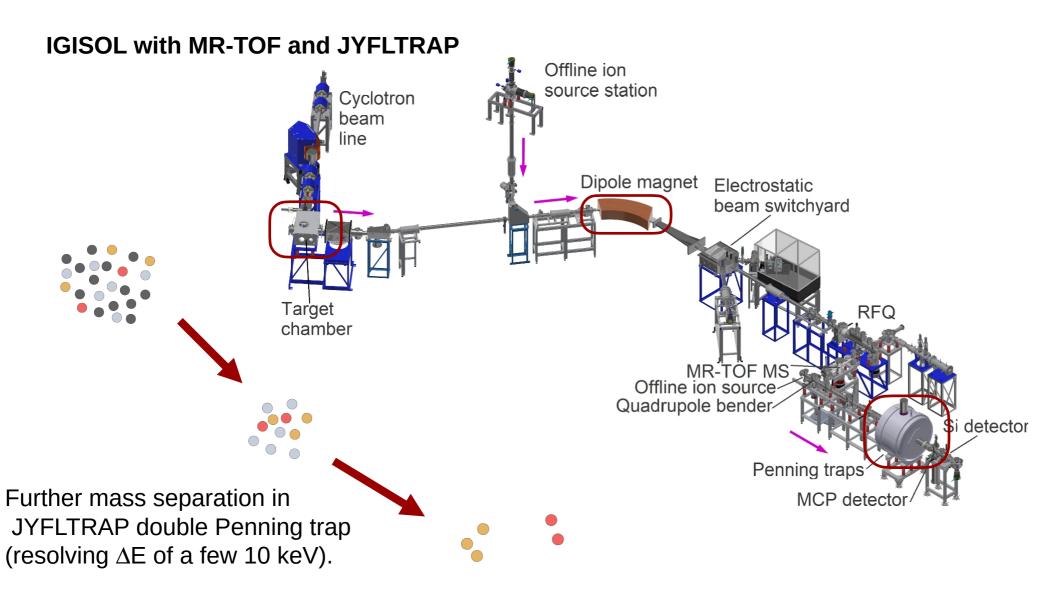






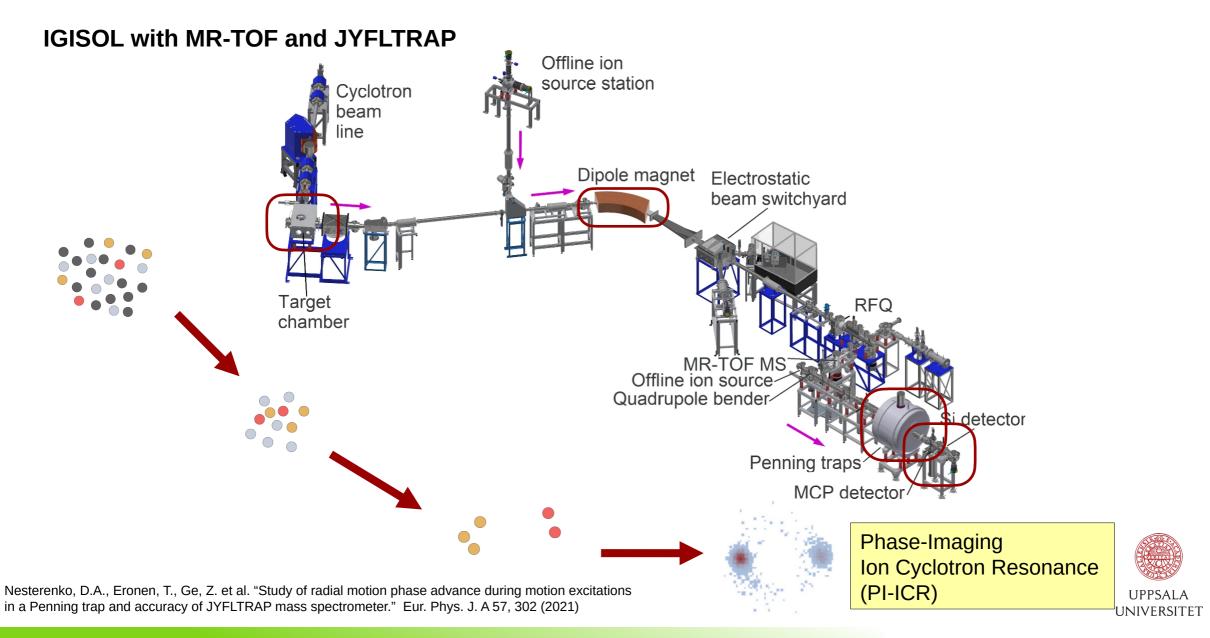


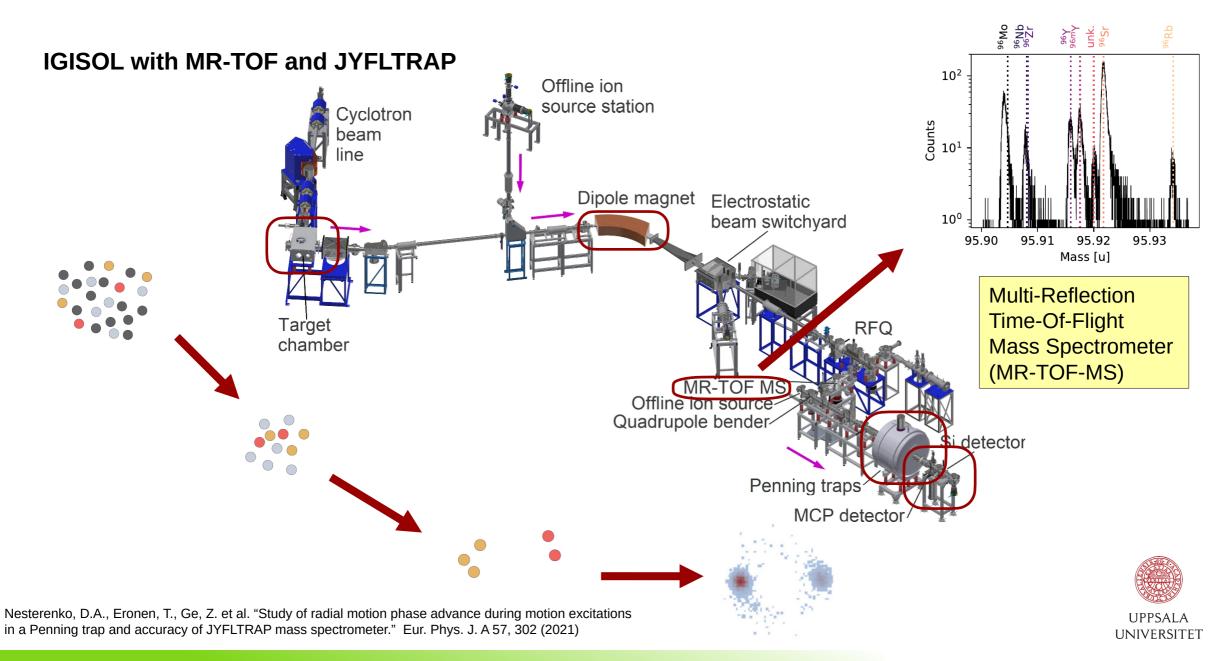
Nesterenko, D.A., Eronen, T., Ge, Z. et al. "Study of radial motion phase advance during motion excitations in a Penning trap and accuracy of JYFLTRAP mass spectrometer." Eur. Phys. J. A 57, 302 (2021)





Nesterenko, D.A., Eronen, T., Ge, Z. et al. "Study of radial motion phase advance during motion excitations in a Penning trap and accuracy of JYFLTRAP mass spectrometer." Eur. Phys. J. A 57, 302 (2021)





#### The phase-imaging ion-cyclotron-resonance technique (PI-ICR) is powerful!

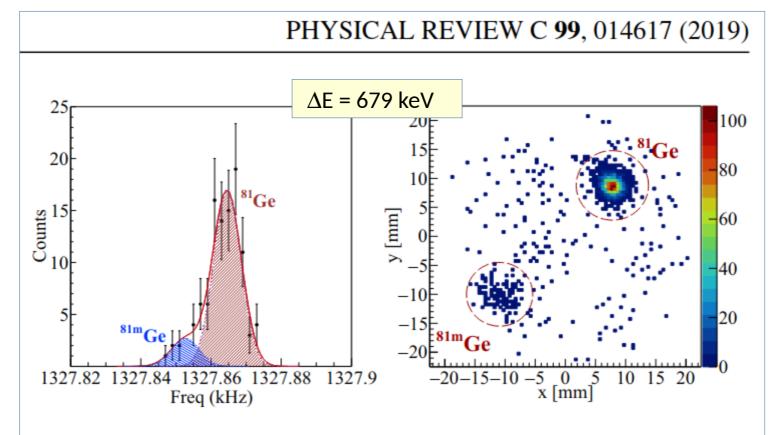


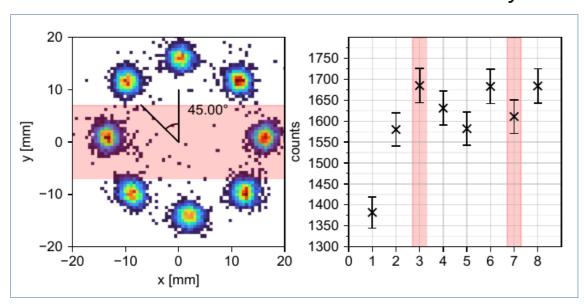
FIG. 1. The case of <sup>81</sup>Ge, observed with the sideband cooling technique (left) and with the PI-ICR technique (right). The dashed circles are used to guide the eye.

By now we have a MRP of about 10<sup>7</sup> and can resolve <sup>129</sup>Sn (35 keV)

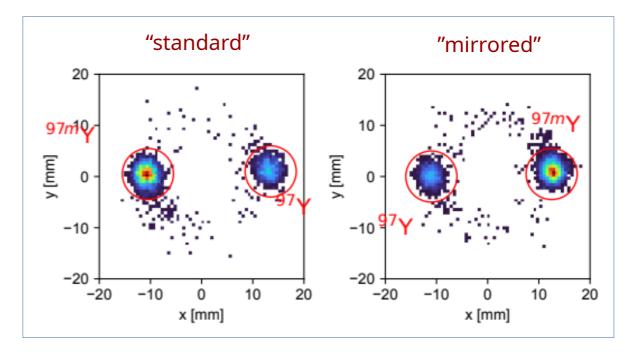


#### Main corrections: efficiency of the multi-channel plate (MCP) detector

#### Measurement of rel. detection efficiency



Stable offline ion beam impinges the MCP (for same amount of time) at different positions.



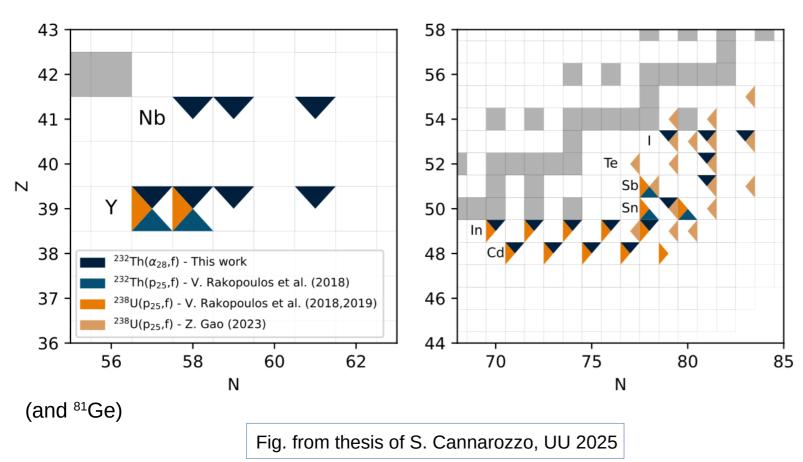
Two positions are selected and measurements
Are repeated with flipped positions of the ion spots
To cancel out efficiency differences as much as possible.

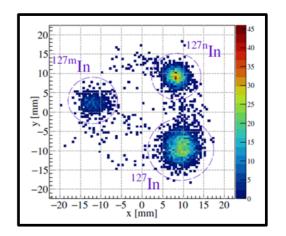


S. Cannarozzo et al., EPJ Web Conf. 322, 08007 (2025) (Proceedings of CNR\*24)

#### **Nuclei with IYR data from IGISOL**

So far 37 IYR measured; several for multiple fissioning systems:





Several campaigns over the past years:

<sup>232</sup>Th(p,f) and <sup>238</sup>U(p,f) at 25 MeV (V. Rakopoulos, Z. Gao)

<sup>232</sup>Th( $\alpha$ ,f) at 28 MeV (S. Cannarozzo)

also some data from

<sup>238</sup>U(n,f) using  $\gamma$ -spectrometry (A. Mattera)



# **Experimental results**

1) IYR from <sup>232</sup>Th(α,f) at 28 MeV and comparison to literature data for IYR from <sup>233</sup>U(n,f) and <sup>235</sup>U(n,f).

2) IYR from  $^{232}$ Th( $\alpha$ ,f) at 28 MeV in the  $^{98}$ Y region.



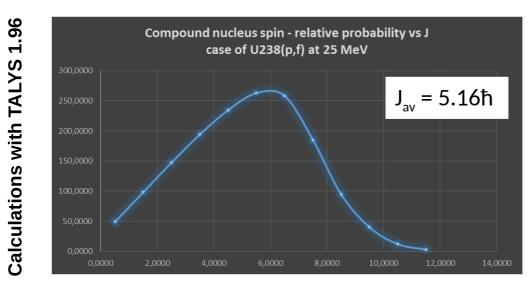
#### IYR from fission using a Penning trap

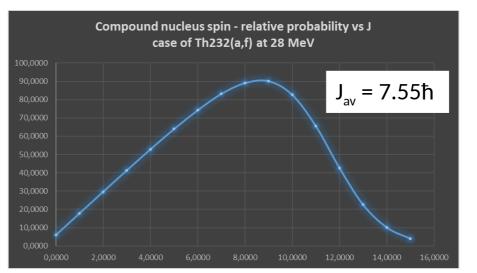
We measured many IYR <sup>238</sup>U(p,f), mainly in the <sup>132</sup>Sn region. (incident proton energy: 25 MeV)

Efforts to obtain IYR from (n,f) ongoing ... (development of new ion guide ongoing)

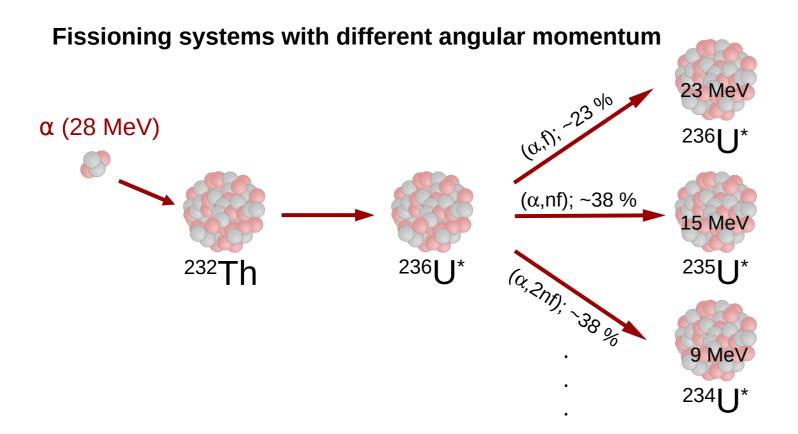
#### Q: What is the impact of the angular momentum of the compound nucleus?

If we can't go down, let's go up and study  $^{232}$ Th( $\alpha$ ,f) and compare to IYR from  $^{233,235}$ U( $n_{th}$ ,f)!



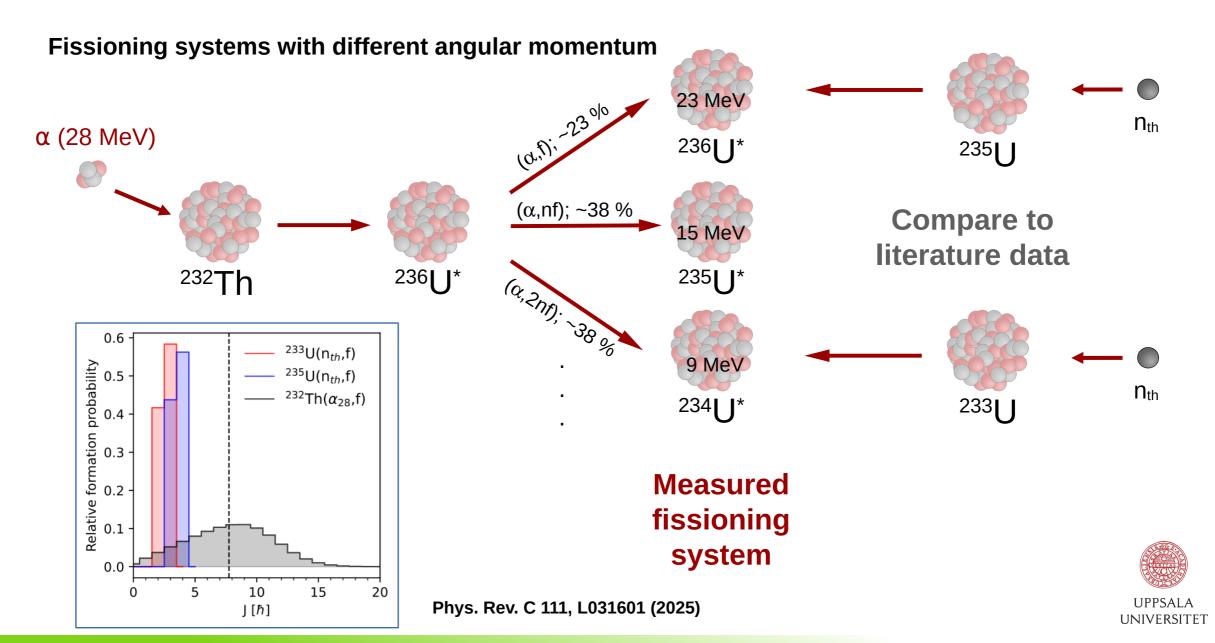




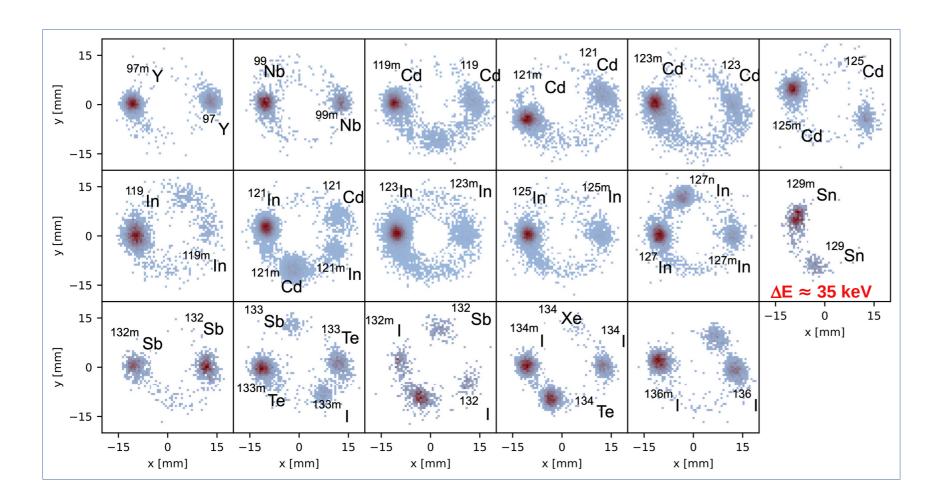


Measured fissioning system





# Results (1) IYR from $^{232}$ Th( $\alpha$ ,f) at 28 MeV



Measured twice at mirrored MCP positions.

Decay corrections applied.

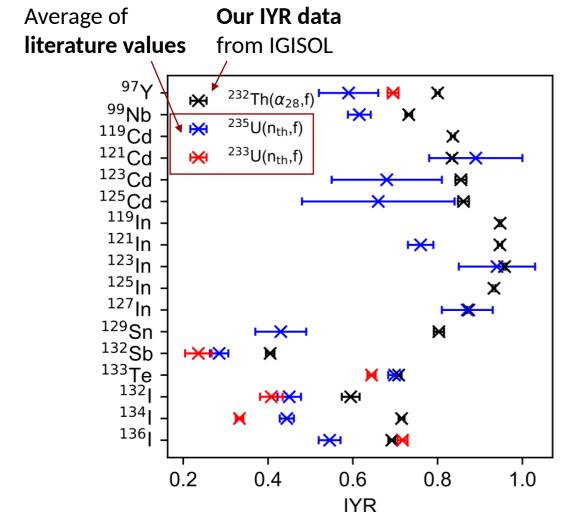
Obtain number of counts in ground and excited isomeric state.

Calculate the IYR. ("high-spin state over total")





# Results (1) IYR from $^{232}$ Th( $\alpha$ ,f) at 28 MeV



Disentangling the influence of excitation energy and compound nucleus angular momentum on fission fragment angular momentum

Simone Cannarozzo \*, \* Stephan Pomp \*, † Andreas Solders \*, Ali Al-Adili \*, Zhihao Gao \*, and Mattias Lantz \*, Department of Physics and Astronomy, Uppsala University, Box 516, 751 20 Uppsala, Sweden

Heikki Penttilä \*, Anu Kankainen \*, Iain Moore \*, Tommi Eronen \*, Zhuang Ge \*, Jouni Ruotsalainen, Maxime Mougeot \*, Ville Virtanen \*, Arthur Jaries \*, Marek Stryjczyk \*, and Andrea Raggio \*, Department of Physics, Accelerator Laboratory, University of Jyvaskyla, P.O. Box 35 (YFL), 40014 Jyvaskyla, Finland

(Received 6 December 2024; revised 28 January 2025; accepted 7 March 2025; published 26 March 2025)

Compound nucleus angular momentum is about 7.5 ħ.

Impact on IYR?

Compare to  $^{233,235}$ U( $n_{th}$ ,f) (with  $\sim 3$  ħ). Average increased IYR.

We conclude that a significant part (at least 40%) of the extra CN spin goes to the FF.

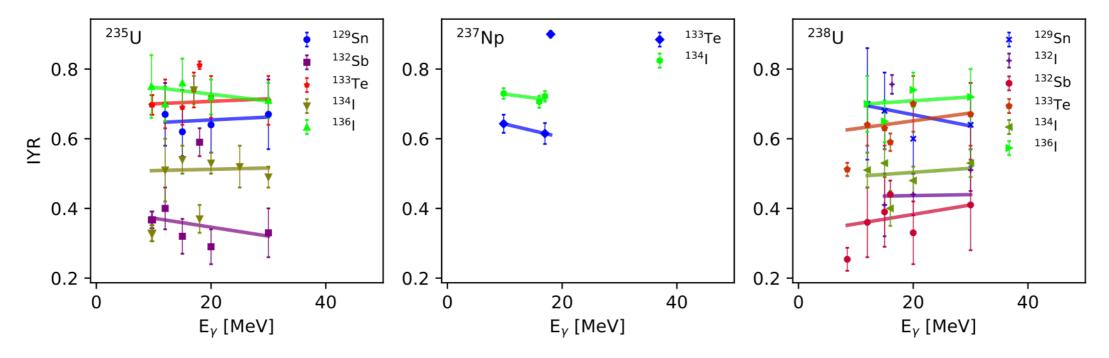
(remaining part likely goes to orbital ang. momentum)

Could this not be due to the excitation energy? We think not ...



## **Results (1)** Impact of excitation energy?

• Photo-fission literature data was used to study influence of compound nucleus excitation energy on IYRs.

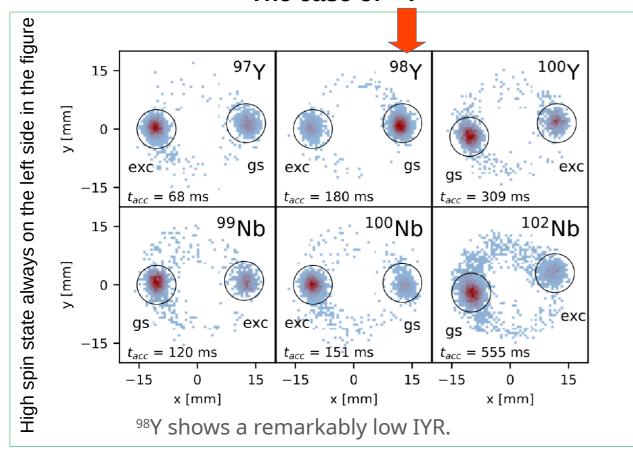


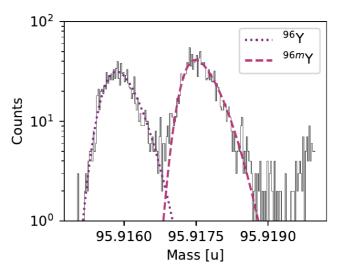
•  $\Delta IYR/\Delta E = 0.0001(5) \text{ MeV}^{-1}$  No significant dependence of the IYRs on the incident y-ray energy.



S. Cannarozzo et al., PRC **111** L031601 (2025)

Results (2) IYR from  $^{232}$ Th( $\alpha$ ,f) at 28 MeV The case of  $^{98}$ Y





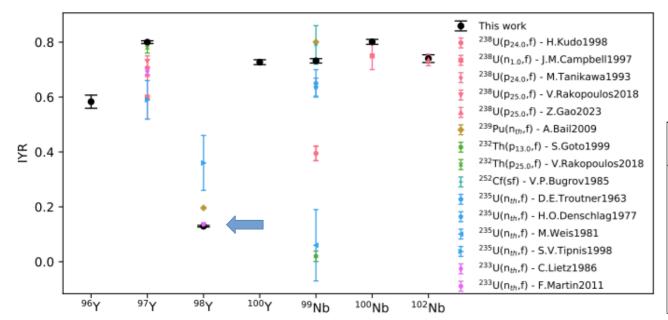
	Ground state		Excited state			
Nuclide	$t_{1/2}$ (s)	$\mathrm{I}^{\pi}$	$t_{1/2}$ (s)	$\mathrm{I}^{\pi}$	$E_x$ (keV)	IYR
<sup>96</sup> Y	5.34(5)	0-	9.6(2)	8+	1540.5(4)	0.58(2)
<sup>97</sup> Y (*)	3.75(3)	$1/2^{-}$	1.17(3)	9/2+	667.52(23)	0.800(5)
$^{98}Y$	0.548(2)	$0_{-}$	2.32(8)	$(6^+, 7^+)$	465.7(7)	0.129(4)
$^{100}{ m Y}$	0.94(3)	4+	0.727(6)	1+	144(16)	0.727(9)
<sup>99</sup> Nb (*)	15.0(2)	9/2+	150(12)	1/2-	365.27(8)	0.732(9)
$^{100}$ Nb	1.5(2)	1+	2.99(11)	$(5^{+})$	313(8)	0.80(1)
<sup>102</sup> Nb	4.3(4)	$(4^{+})$	1.31(16)	$(1^{+})$	94(7)	0.74(1)

**State ordering** of <sup>98</sup>Y, <sup>100</sup>Y, <sup>100</sup>Nb, <sup>102</sup>Nb verified.

Confirms NUBASE2020; i.e. reversed order of <sup>100</sup>Y in ENSDF.

S. Cannarozzo et al., submitted to PLB; 2504.11274v3





Outlier reason?

98Y known for large isomeric shift
But how to explain?
State ordering experimentally verified!

	Ground state		Excited state			
Nuclide	$t_{1/2}$ (s)	$\mathbf{I}^{\pi}$	$t_{1/2}$ (s)	$\mathrm{I}^{\pi}$	$E_x$ (keV)	IYR
<sup>96</sup> Y	5.34(5)	0-	9.6(2)	8+	1540.5(4)	0.58(2)
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<sup>102</sup> Nb	4.3(4)	$(4^{+})$	1.31(16)	$(1^{+})$	94(7)	0.74(1)

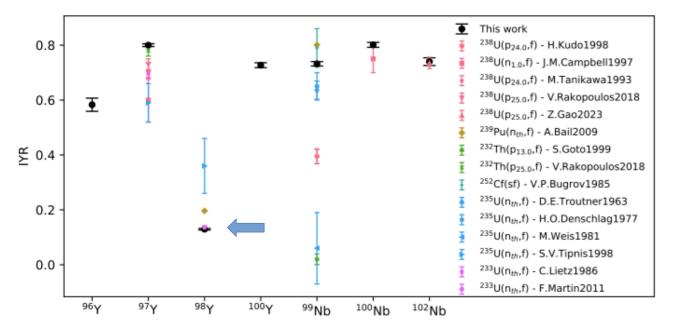
<sup>98</sup>Y shows a remarkably low IYR.

**State ordering** of <sup>98</sup>Y, <sup>100</sup>Y, <sup>100</sup>Nb, <sup>102</sup>Nb verified.

#### Confirms NUBASE2020; i.e. reversed order of <sup>100</sup>Y in ENSDF.

S. Cannarozzo et al., submitted to PLB; 2504.11274v3





No other cases of such low IYR known.

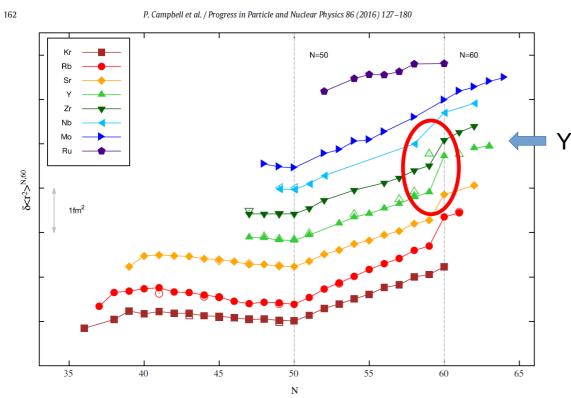
The earlier reported low IYR for <sup>114</sup>Rh was due to wrong spin ordering.

M. Stryjczyk et al., "Discovery of a new long-lived isomer in <sup>114</sup>Rh via Penning-trap mass spectrometry" Phys. Lett. B **862**, 139359 (2025).

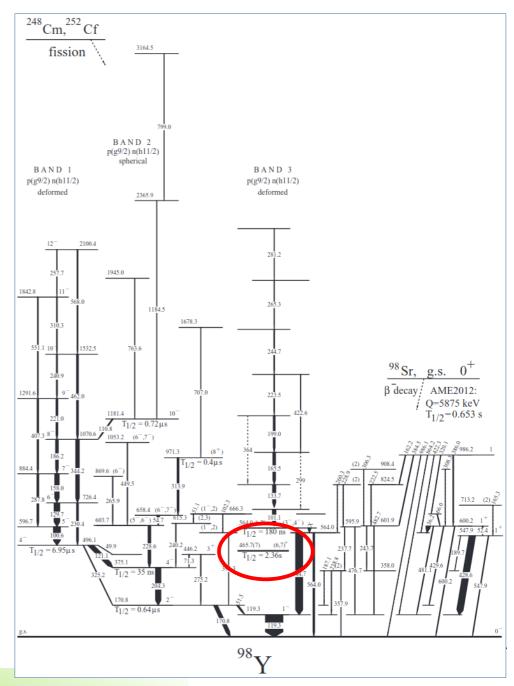
One case with IYR  $\approx$  0.27 is <sup>133</sup>I, but spins of the isomeric pairs are 7/2 and 19/2.

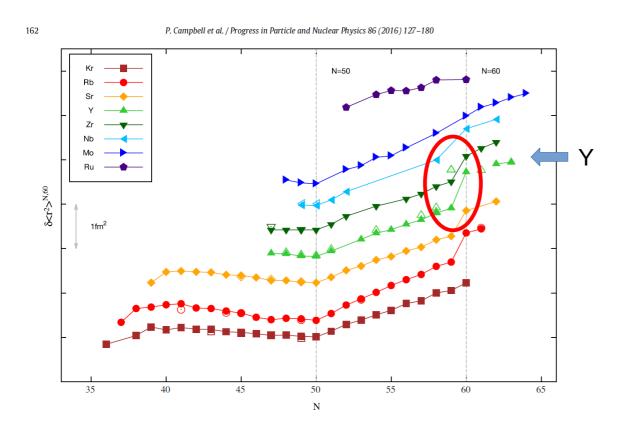


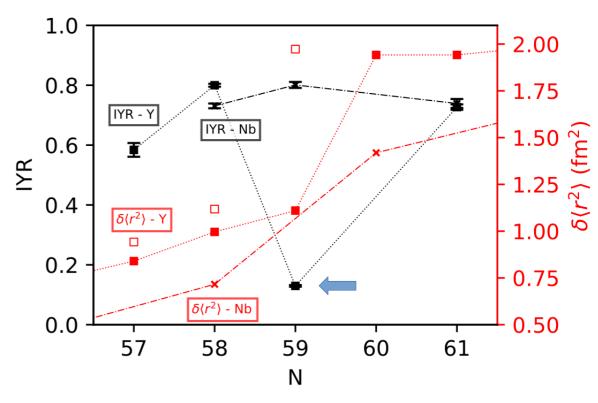
S. Cannarozzo et al., submitted to PLB; 2504.11274v3



- 98Y shows a large isomeric shift (also 79Zn)
- Shape co-existence
- Isomer rarely populated in fission









S. Cannarozzo et al., submitted to PLB

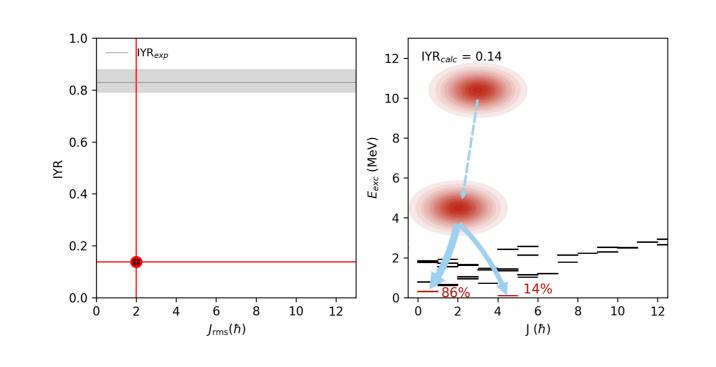
#### Fission and isomers – relevance for other field



"The sensitivity study identified  $^{98}$ Y, shown in Fig. 4(b), as the fission product whose newly evaluated IYR has the greatest impact on the  $\nu_e$  spectrum, accounting for an increase of over 20% at 8 MeV for  $^{235}$ U thermal fission. This can be explained as the experimental IYR [13.9(6)%] recommended in Ref. [48] corresponding to a substantial inversion of the population of isomer and ground state compared to the value used in evaluated libraries and based on the Madland & England model, which predicts a IYR of 81%." (my emphasis)



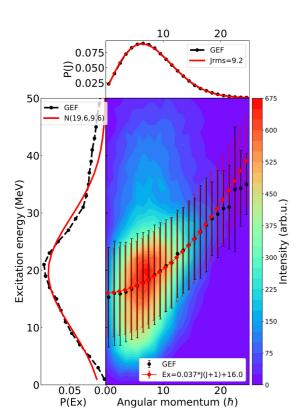
# From IYR to fission fragment angular momenta (VERY brief)



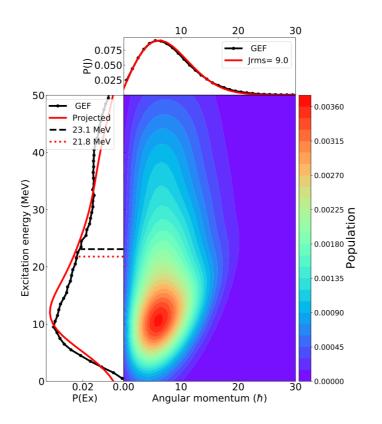


# **Angular momentum estimation – Example of <sup>133</sup>Te**

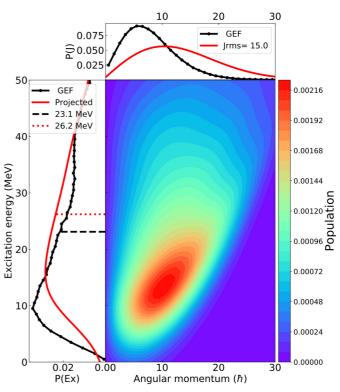
Fit to GEF data for each fission channel.

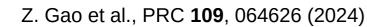


Weighted sum of matrices for 'all' fission channels.



Creation of new matrices for any  $J_{rms}$ 



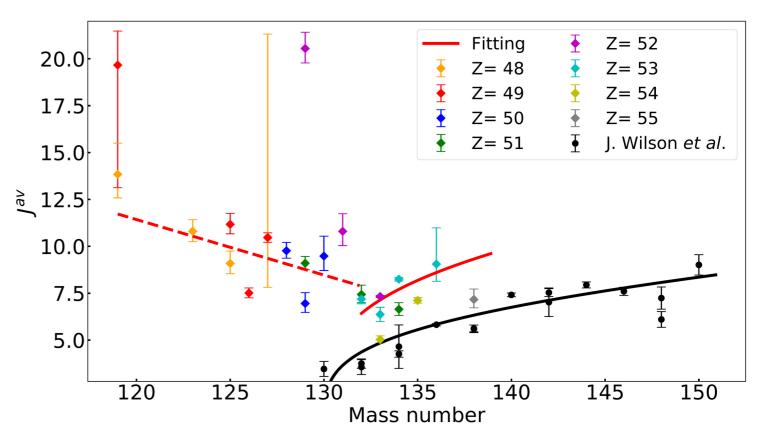




#### Comparing derived Jrms from <sup>238</sup>U(p,f) at 25 MeV with the data from Wilson et al.

- Comparison to Wilson data for <sup>238</sup>U(n<sub>th</sub>,f).

  J. Wilson et al., Nature **590**, 566 (2021)
- Overall larger average angular momenta. (Supports our  $^{232}$ Th( $\alpha$ ,f) study)
- Minimum angular momentum: A ≈ 130.



Gao et al., Phys. Rev. C 109, 064626 (2024)



#### **Summary and outlook**

Over the past years we measured IYR for 37 nuclei at IGISOL.

Recently we studied **IYR from**  $^{232}$ **Th**( $\alpha$ ,**f**) and show that:

- 1) Increased **CN angular momentum** i.e. added CN angular momentum leads to higher fission fragment angular momentum
- 2) Using literature data, we find **no significant dependence on excitation energy**.
- 3) We highlight the unusual IYR for 98Y (and establish/verify state ordering of 4 Y and Nb isotopes).

#### Furthermore:

4) The IYR can be used to **derive J**<sub>rms</sub> of the fission fragment (model dependent).



#### **Summary and outlook**

#### Plans:

- A) Additional IYR measurements from  $^{232}$ Th( $\alpha$ ,f) at IGISOL in the symmetry and low mass region.
- B) IYR from spontaneous fission of the 0<sup>+</sup> nuclei <sup>248</sup>Cm and <sup>252</sup>Cf FRS-CSC at GSI, Germany.
- C) Continue development of **methods to derive fragment angular momenta** from the IYR.
- D) Develop a **new ion guide** with increased efficiency to allow for measuring **(n,f)** at IGISOL.

In this context the output from the new IAEA CRP on nuclear level densities will be valuable.



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